

Chapter **5**

COMPLEX NUMBERS

Note:

$x + iy = (x, y)$ is called rectangular form of the complex number. Henceforth $x + iy$ means (x, y) . We denote this by single letter z .

Integral powers of i :

$$1) \quad i^2 = i \cdot i = \sqrt{-1}\sqrt{-1} = (\sqrt{-1})^2 = -1$$

$$2) \quad i^3 = i^2 \cdot i = (-1)i = -i$$

$$3) \quad i^4 = (i^2)^2 = (-1)^2 = 1$$

$$4) \quad i^5 = i^4 \cdot i = 1 \cdot i = i \text{ and so on}$$

Then i^n ($n \in \mathbb{Z}$) always given one of the four values $-1, -i, 1, i$.

Note:

$$1) \quad i^{4n} = 1$$

$$2) \quad i^{4n+1} = i \quad (n \in \mathbb{Z})$$

$$3) \quad i^{4n+2} = -1$$

$$4) \quad i^{4n+3} = -i$$